

**At the end of this chapter you should be able to**

1. Transform equations written in the natural variables of an applied problem to the canonical  $Ax = b$  of linear algebra.
2. Explain the condition of consistency in terms of linear combinations of column vectors.
3. Explain the condition of singularity of an  $n \times n$  matrix in terms of linear independence.
4. Express matrix rank as a measure of linear independence.
5. Relate rank of the coefficient matrix to the consistency of a  $n \times n$  system of equations.
6. Solve a small system of linear equations using Gaussian elimination
7. Describe the most efficient procedures for solving  $Lx = b$  or  $Ux = b$  when  $L$  is lower triangular and  $U$  is upper triangular.
8. Describe the significance of  $\kappa(A)$  on the reliability of the numerical solution to  $Ax = b$ .
9. Describe the reason for pivoting. Is pivoting a remedy for ill-conditioned systems?
10. Write (describe) a procedure for solving  $Ax = b$  given an LU factorization of  $A$ .

*Note:* Sections of Chapter 8 *not* covered (and hence, you are not responsible for) are 8.4.2 (Cholesky factorization) and 8.5 (Nonlinear Systems of Equations)